Chapter 6:Work and Energy

Lecture 1 The University of Jordan/Physics Department Prof. Mahmoud Jaghoub

6-1] Work done by a constant force.

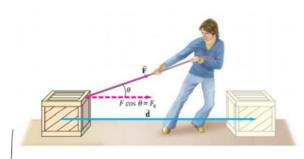
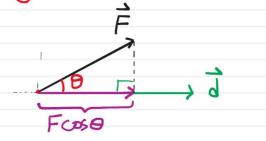


FIGURE 6–1 A person pulling a crate along the floor. The work done by the force $\vec{\mathbf{F}}$ is $W = Fd \cos \theta$, where $\vec{\mathbf{d}}$ is the displacement.

To move the box a displacement I to the right as shown in the figure, work must be done thow to define what is meant by work?

Work done = magnitude of the displacement times
the component of the force parallel to
the displacement.

Work W = (F cos0) d = Fdcos0



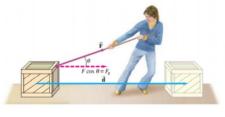
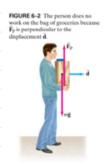


FIGURE 6-1 A person pulling a crate along the floor. The work done by the force $\vec{\mathbf{F}}$ is $W = Fd \cos \theta$, where $\vec{\mathbf{d}}$ is the displacement.



In the figure the work done by the man is zero, because his force is perpendicular to the displacement (0=90°)

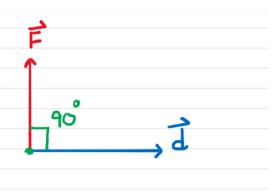


O: smaller angle between F and I when they originate from the same point.

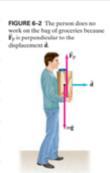
NOTE: Work is a scalar quantity-

When does the work done by a Force F has a value of zero?





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Unit of Work:

unit > [W] = N·m = Joule

of oik

IJ = IN·lm

When a force of IN acts
on an object and moves
it a distance of Ima log hte
direction of the force > the
work done is 1 Jove.

Example:

In the figure the box moves a distance of 10m to the right.

 $f_{k}=30 \text{ Newtons}$ F=100 Newtons d=10 m

V

(i) Find the work done by each force.

WN = Nd Cos(900) =0

Way = mg d cos(90°) =0

F moves the object

WF = Fd cos(0) = (100) (10)(1) = 1000 J. (NOTE WYO)

WF = fk d cos 180° = (30)(10)(-1) = -300 J. (NOTE WYO) of the box.

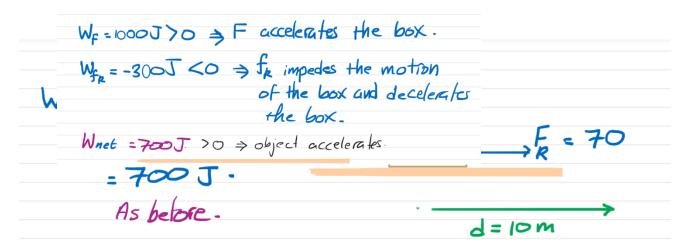
Note: the work of Friction is negative. BUT work is a scalar and NOT a vector. The sign here does NOT mean direction.

(ii) Find the net (total) work done on the box.

$$W_{net} = W_{N} + W_{Mg} + W_{F} + W_{fk}$$

= 0 + 0 + 1000 + (-300) = 700 J.
Alternatively:

$$\rightarrow_+ F_R = F - f_R = 100 - 30 = 70$$
 Newtons in the positive or-direction. \uparrow NoTE: \uparrow NoTE: \uparrow N-my=0.



A resultant force acts on the box in the positive x-direction > the box accelerates along the positive x-direction. Remember the net work done on the object is positive.

What does the sign of the work clone on an object mean?

What >0 (1.e positive) > object accelerates

What <0 (1.e negative) > object decelerates

W=0 > object moves at constant speed.

$$W_{f} = 1000J > 0 \Rightarrow F$$
 accelerates the box.

$$W_{f_R} = -300J < 0 \Rightarrow f_R$$
 impedes the motion of the box and decelerates the box.

Wnet = 700 J > 0 > object accelerates.

Example: Find the net work done on the box.

$$V_{N} = W_{Mg} = 0$$

$$W_{f} = (60)(5) \cos 180 = -100J$$

$$W_{net} = 150 - 100 = 50J$$

EXAMPLE 6-2 Work on a backpack. (a) Determine the work a hiker must do on a 15.0-kg backpack to carry it up a hill of height h = 10.0 m, as shown in Fig. 6-4a. Determine also (b) the work done by gravity on the backpack, and (c) the net work done on the backpack. For simplicity, assume the motion is smooth and at constant velocity (i.e., acceleration is zero).

APPROACH We explicitly follow the steps of the Problem Solving Strategy above. SOLUTION

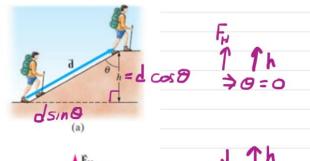
- Draw a free-body diagram. The forces on the backpack are shown in Fig. 6-4b: the force of gravity, $m\mathbf{g}$, acting downward; and \mathbf{F}_H , the force the hiker must exert upward to support the backpack. The acceleration is zero, so horizontal forces on the backpack are negligible.
- 2. Choose a coordinate system. We are interested in the vertical motion of the backpack, so we choose the y coordinate as positive vertically upward.
- 3. Apply Newton's laws. Newton's second law applied in the vertical direction to the backpack gives (with $a_v = 0$)

$$\Sigma F_y = ma_y$$

So, $F_H - mg = 0$.
 $F_H = mg = (15.0 \text{ kg})(9.80 \text{ m/s}^2) = 147 \text{ N}$.

$$F_{\rm H} = mg = (15.0 \,\text{kg})(9.80 \,\text{m/s}^2) = 147 \,\text{N}.$$

FIGURE 6-4 Example 6-2.





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So.

$$F_{\rm H} = mg = (15.0 \,\text{kg})(9.80 \,\text{m/s}^2) = 147 \,\text{N}.$$

4. Work done by a specific force. (a) To calculate the work done by the hiker on the backpack, we use Eq. 6-1, where θ is shown in Fig. 6-4c,

$$W_{\rm H} = F_{\rm H}(d\cos\theta),$$

and we note from Fig. 6-4a that $d \cos \theta = h$. So the work done by the hiker is

$$W_{\rm H} = F_{\rm H}(\underline{d\cos\theta}) = F_{\rm H}\underline{h} = mgh = (147 \,{\rm N})(10.0 \,{\rm m}) = 1470 \,{\rm J}.$$

The work done depends only on the elevation change and not on the angle of the hill, θ . The hiker would do the same work to lift the pack vertically by height h. (b) The work done by gravity on the backpack is (from Eq. 6-1 and Fig. 6-4c)

$$W_G = mg d \cos(180^\circ - \theta).$$

Since $cos(180^{\circ} - \theta) = -cos \theta$ (Appendix A-7), we have

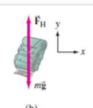
$$W_G = mg(-d\cos\theta)$$

= -mgh
= -(15.0 kg)(9.80 m/s²)(10.0 m) = -1470 J.

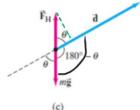
NOTE The work done by gravity (which is negative here) does not depend on the angle of the incline, only on the vertical height h of the hill.

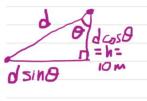
5. Net work done. (c) The net work done on the backpack is $W_{\text{net}} = 0$, because the net force on the backpack is zero (it is assumed not to accelerate significantly). We can also get the net work done by adding the work done by each force:

$$W_{\text{net}} = W_{\text{G}} + W_{\text{H}} = -1470 \,\text{J} + 1470 \,\text{J} = 0.$$







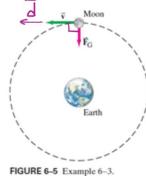


mgd cos(180-0) = - mgd cos0

PROBLEM SOLVING Work done by gravity depends on height of hill (not on angle)

moon o ib, its the earth of constant speed.

Rale



CONCEPTUAL EXAMPLE 6-3 Does the Earth do work on the Moon? The Moon revolves around the Earth in a nearly circular orbit, kept there by the

gravitational force exerted by the Earth. Does gravity do (a) positive work, (b) negative work, or (c) no work on the Moon?

RESPONSE The gravitational force $\vec{\mathbf{F}}_G$ exerted by the Earth on the Moon (Fig. 6-5) acts toward the Earth and provides its centripetal acceleration, inward along the radius of the Moon's orbit. The Moon's displacement at any moment is tangent to the circle, in the direction of its velocity, perpendicular to the radius and perpendicular to the force of gravity. Hence the angle θ between the force $\vec{\mathbf{F}}_{\mathrm{G}}$ and the instantaneous displacement of the Moon is 90°, and the work done by gravity is therefore zero ($\cos 90^{\circ} = 0$). This is why the Moon, as well as artificial satellites, can stay in orbit without expenditure of fuel: no work needs to be done against the force of gravity.

F towards the center of the

d is alway perpendicular to F

30=90°

Wnot= 0

W=Fdcos0

xx-axis

6-2] Work done by a variable force.

A box moves along the

2-axis under the effect

of a variable force

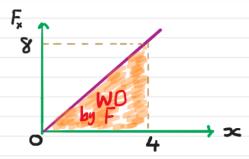
variable force

 $F_{x} = 2x$.

Find the work done by Ex when the box

Moves from $x = 0 \text{ m} \rightarrow x = 4 \text{ m}$.

W = Area under the curve



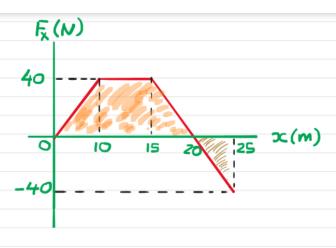
For F. - x graph area under the curve gives the work

Example: An object moves along the oc-axis under a variable force F_x as shown in the F_i gure.

Find the work done on the box by Fx over the following intervals:

i)
$$x = 6 \rightarrow 20 \text{ m}$$

 $W_1 = \frac{1}{2} (5 + 20)(40) = 500 \text{ J}$



- ii) $2c = 20 \rightarrow 25 \text{ m}$ $W = \frac{1}{2} (5)(-40) = -100 \text{ J}$
- iii) Find the not work done on the box by F_X . $W_{net} = W_1 + W_2 = 500 - 100 = 400 J$.