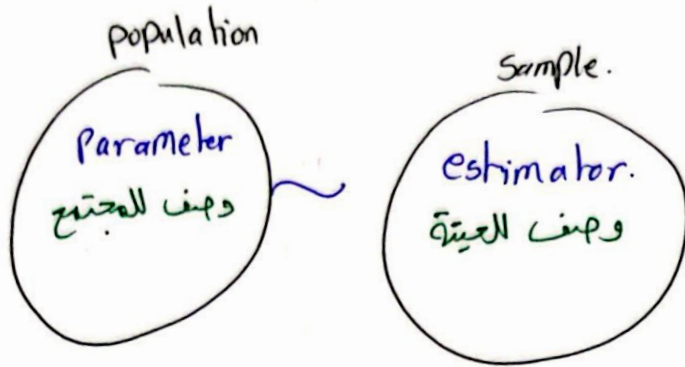


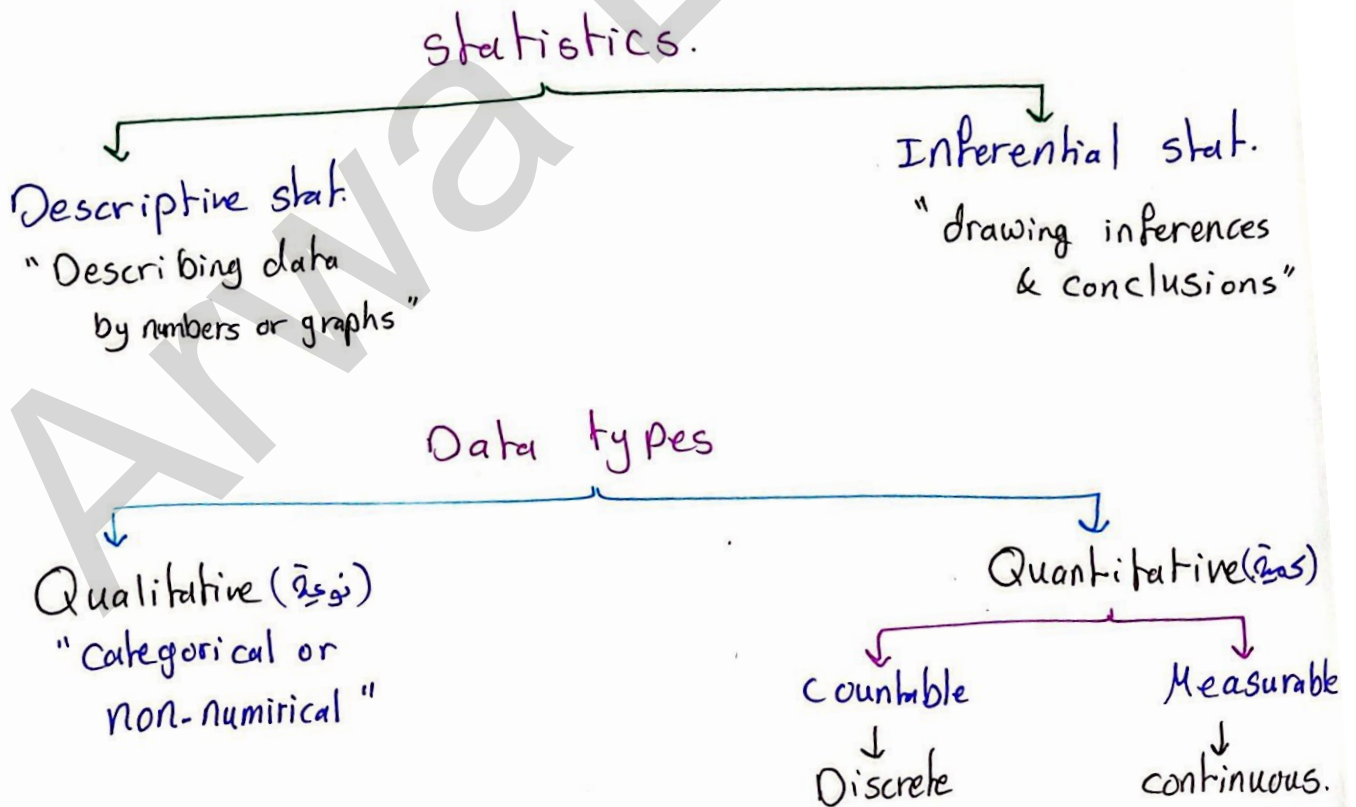
\* Chapter (1) Full-Summary :

Data sets  $\left\{ \begin{array}{l} \rightarrow \text{Population.} \rightarrow \text{كل المجتمع} \\ \rightarrow \text{sample} \rightarrow \text{جزء من المجتمع} \end{array} \right.$

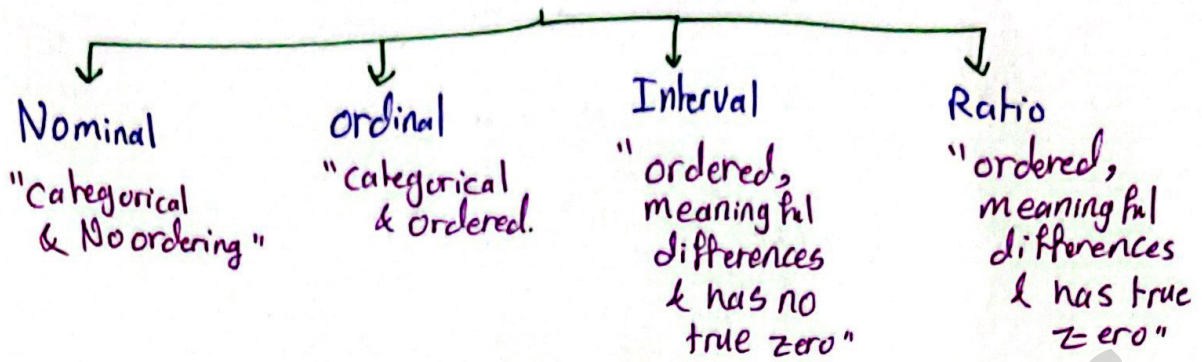
→ We have two important terms :



\* estimator (statistic) may change by changing the sample taken but parameter remain the same for the population.



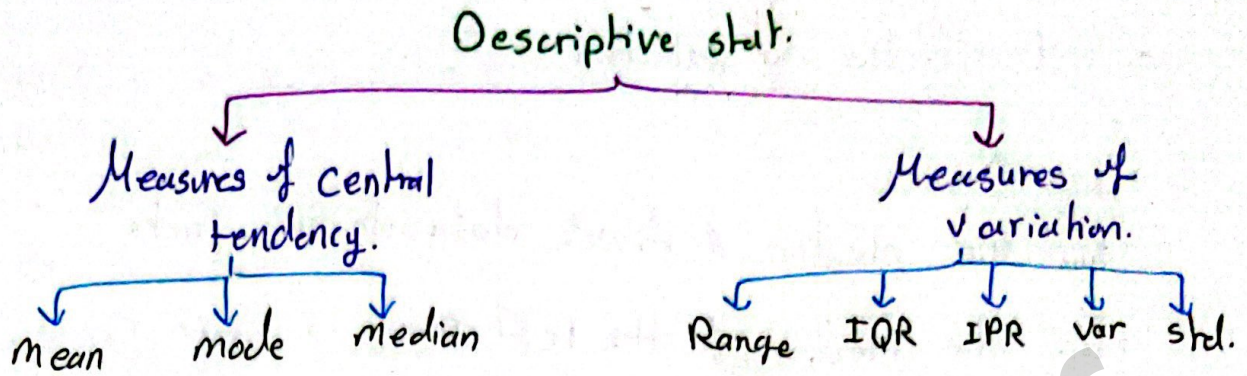
# Measurement scales



Level	Put data in category	Arrange data values	Subtract data values	Write values as multiple from each other
Nominal	Yes	No	No	No
Ordinal	Yes	Yes	No	No
Interval	Yes	Yes	Yes	No
Ratio	Yes	Yes	Yes	Yes.

← مهم فيتر الجدول .

\* chapter (2): Descriptive statistics (Full-summary).



\* Measures of central tendency :-

1] The Mean :-  $\rightarrow$  Affected by outliers.

1. Raw data                      2. stem & leaf.

$$\bar{x} = \frac{\sum x_i}{n}$$

3. Frequency dis.:-

$\rightarrow$  add  $f \cdot x$ , then :

$$\bar{x} = \frac{\sum f \cdot x}{n}, \quad [n = \sum f]$$

Weighted mean:

$$\bar{x} = \frac{\sum X \cdot w}{\sum w}$$

4. grouped frequency distribution:-

$\rightarrow$  add  $x = \text{midpoint} = \frac{L + U}{2}$ .

$\rightarrow$  add  $f \cdot x$ , then :-

$$\bar{x} = \frac{\sum f \cdot x}{n}, \quad [n = \sum f]$$

Note :  $\sum x_i = n \cdot \bar{x}$ .

2] The Mode :  $\rightarrow$  the best when data is qualitative

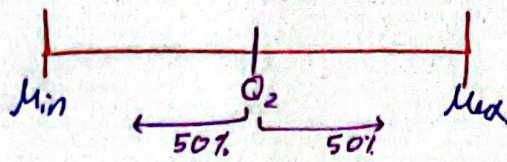
1. Raw data      2. stem & leaf      3. Frequency dis.:

$\rightarrow$  take the value that occurs mostly. 1]

4. grouped frequency dis.:

Class of maximum freq.  $\rightarrow$  modal class & mod is the midpoint

### 3 The Median ( $Q_2$ ):



The value in the middle of data set & not affected by outliers.

#### 1. Raw data :-

→ Arrange data values.

$$\rightarrow Q_2 = \frac{n}{2} \begin{cases} \text{fraction} \rightarrow \text{next int} \\ \text{whole no.} \rightarrow \frac{k^{\text{th}} + (k+1)^{\text{th}}}{2} \end{cases}$$

#### 2. stem & leaf :-

data is arranged & use same formula & steps.

#### 3. frequency distribution :-

→ Add c.f & Intervals. (c.f is  $\leq$  &  $<$ )

$$\rightarrow Q_2 = \frac{n}{2} \begin{cases} \text{fraction} \rightarrow \text{next int} \\ \text{whole no.} \rightarrow \frac{k^{\text{th}} + (k+1)^{\text{th}}}{2} \end{cases}$$

#### 4. grouped frequency distribution :-

→ Add c.f & URB.

$$\rightarrow Q_2 = \frac{n}{2}. \text{ (Don't Apply The Rule)}$$

\* Note :- class length = C.L = URB - LRB.

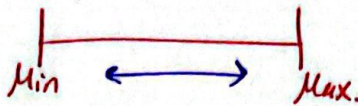
\* The Relative frequency :-

$$\boxed{1} R.f = \frac{f}{\Sigma f}$$

$$\boxed{2} \Sigma R.f = 1 \rightarrow 1 = \text{مجموع نسبته قيمه}$$

\* Measures of Variation :-

$\boxed{1}$  The Range :-



1. Raw data + 2. stem & leaf + 3. frequency distribution

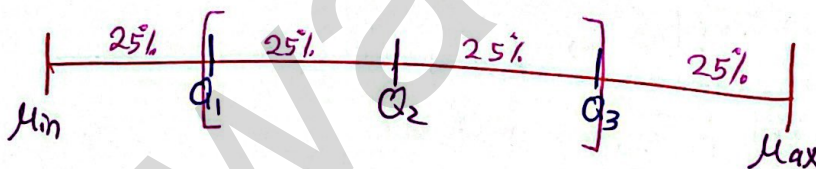
$$\text{Range} = \text{Max} - \text{Min}$$

4. grouped frequency distribution :-

$$\text{Range} = \text{Max}(URB) - \text{Min}(LRB)$$

\* Range is affected by outliers.

$\boxed{2}$  Inter-quartile - range (IQR) :-



→ takes the 50% of data that falls in the middle.

→ not affected by outliers.

$$\rightarrow IQR = Q_3 - Q_1$$

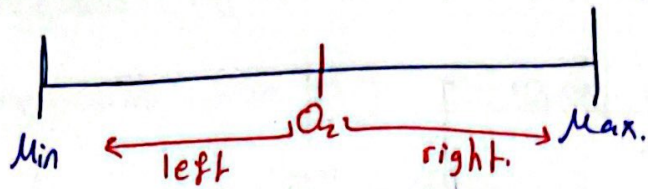
$Q_1$  : 1<sup>st</sup> quartile (lower) , 25% of data below it.

$Q_3$  : 3<sup>rd</sup> quartile (upper) , 75% of data below it

$$\text{Mid quartile} = \frac{Q_3 + Q_1}{2}$$

$\boxed{3}$

1. Raw data :



الطريقة  
الجديدة و  
المعتادة.

find the median of left part  $\rightarrow$  call it  $Q_1$

find the median of right part  $\rightarrow$  call it  $Q_3$ .

2. Stem & leaf :

\* تحويل الجدول إلى Raw data والبقاء نفس خطوات Raw data \*

3. Frequency distribution :

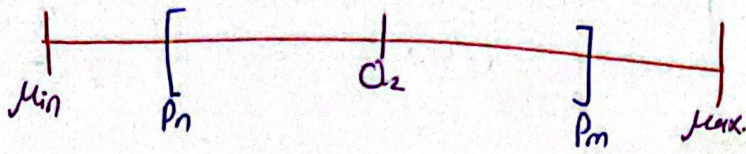
$\rightarrow$  Add c.f & Intervals.

$\rightarrow Q_1 = \frac{n}{4}$  Fraction  $\rightarrow$  next int.

$Q_3 = \frac{3n}{4}$  whole no.  $\rightarrow \frac{k^{th} + (k+1)^{th}}{2}$

$IQR = Q_3 - Q_1$

### 3] Inter-Percentile - range (IPR) :-



$$IPR = P_m - P_n \quad \rightarrow \text{هو الفرق بين أي نسبتين}$$

\* Percentile ( $P_k$ ) :-

1. Raw data :-

→ Arrange data values.

$$\rightarrow P_k = \frac{k}{100} \cdot n \quad \left\{ \begin{array}{l} \text{fraction} \rightarrow \text{next int} \\ \text{whole no.} \rightarrow \frac{k^{th} + (k+1)^{th}}{2} \end{array} \right.$$

2. Stem & leaf :-

→ As Raw data, but table give arranged values  
لقيم مرتبة وجاهزة بس لازم نكتب القاعدة.

3. frequency distribution :-

→ Add C.F & Intervals

$$\rightarrow P_k = \frac{k}{100} \cdot n \quad \left\{ \begin{array}{l} \text{fraction} \rightarrow \text{next int} \\ \text{whole no.} \rightarrow \frac{k^{th} + (k+1)^{th}}{2} \end{array} \right.$$

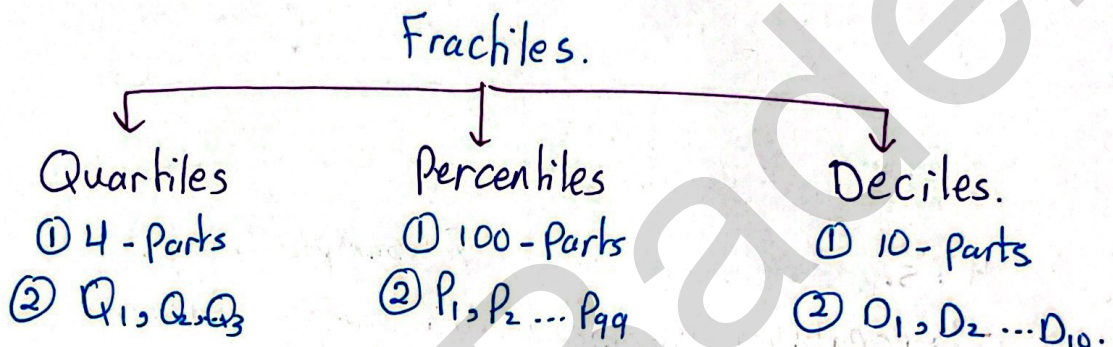
\* Deciles ( $D_k$ ):

We divide data into 10 equal parts:  $D_1, D_2 \dots D_{10}$ .

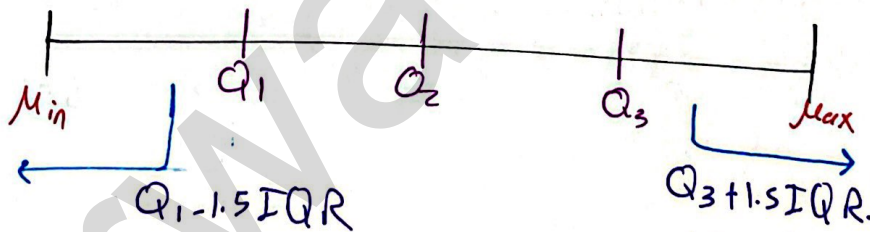
→ كل طريقة من أنواعها على، انهم Percentiles، ويطبق قواينهم

$$D_1 = P_{10}, D_2 = P_{20}, D_3 = P_{30} \dots D_9 = P_{90}.$$

\* Fractiles: numbers divide data into equal parts.



\* Outliers:



less than  $Q_1 - 1.5 IQR$ .

More than  $Q_3 + 1.5 IQR$ .



## 4+5 Variance + standard deviation:

→ Deviation =  $x_i - \bar{x}_i$

→ For sample: var =  $s^2$  & std =  $s$

For population: var =  $\sigma^2$  & std =  $\sigma$ .

1. Raw data & stem & leaf:

Population Variance	Sample Variance.
1) $\sigma^2 = \frac{\sum (x_i - \mu)^2}{N}$	1) $s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$
2) $\sigma^2 = \frac{\sum x^2}{N} - (\mu)^2$	2) $s^2 = \frac{\sum x^2}{n-1} - \frac{(\sum x)^2}{n(n-1)}$
std = $\sigma = \sqrt{\text{Variance}}$	std = $s = \sqrt{\text{Variance}}$
$\mu$ : population mean	$\bar{x}$ : sample mean.
$\sigma^2$ : Population variance	$s^2$ : sample variance.
$N$ : Population size	$n$ : sample size
	* $\sum x^2$ : Sum of squares.

## 3. Frequency distribution.

→ For population:  $\sigma^2 = \frac{\sum f \cdot (x_i - \mu)^2}{N}$

→ الجزء فقط

→ For sample,

$$\boxed{1} \quad s^2 = \frac{\sum f \cdot (x_i - \bar{x})^2}{n-1}$$

$$\boxed{n = \sum f}$$

$$\boxed{2} \quad s^2 = \frac{\sum f \cdot x^2}{n-1} - \frac{(\sum f \cdot x)^2}{n(n-1)}$$

→ Add  $f \cdot x$  /  $x^2$  /  $f \cdot x^2$ .

$$\text{std} = \sqrt{\text{Variance}}$$

**7**

#### 4. grouped frequency distribution :

→ for sample :-

$$1) S^2 = \frac{\sum f \cdot (x_i - \bar{x})^2}{n-1}$$

$$2) S^2 = \frac{\sum f \cdot x^2}{n-1} - \frac{(\sum f \cdot x)^2}{n(n-1)}$$

$$n = \sum f$$

std =  $\sqrt{\text{variance}}$ .

→ Add  $x = \text{mid point} = \frac{\text{lower} + \text{upper}}{2}$ .

→ add  $f \cdot x / x^2 / f \cdot x^2$ .

→ Apply the formula.

\* Note : When all data values the same, all measures of Variation equal zero. \* ما في تمنت \*

Range = IQR = IPR = Variance = std = 0.

#### \* Comparison two collections :

1) Z-score :

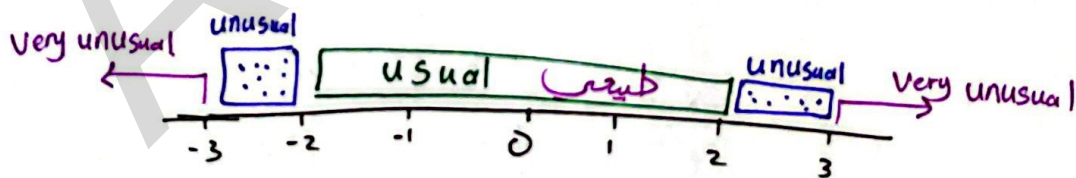
$$Z = \frac{x - \bar{x}}{s}$$

كل ما زاد يكون أفضل.

→ Positive → above the mean.

→ zero → on the mean.

→ Negative → below the mean.



← إذا الطالب جاب Z-score بين -2 و 2 يكون وضع طبيعي  
 ← إذا جاب بين -2 و -3 أو بين 2 و 3 يكون وضع طبيعي  
 ← إذا جاب أقل من -3 أو أكثر من 3 يكون بمررة مت طبيعي.

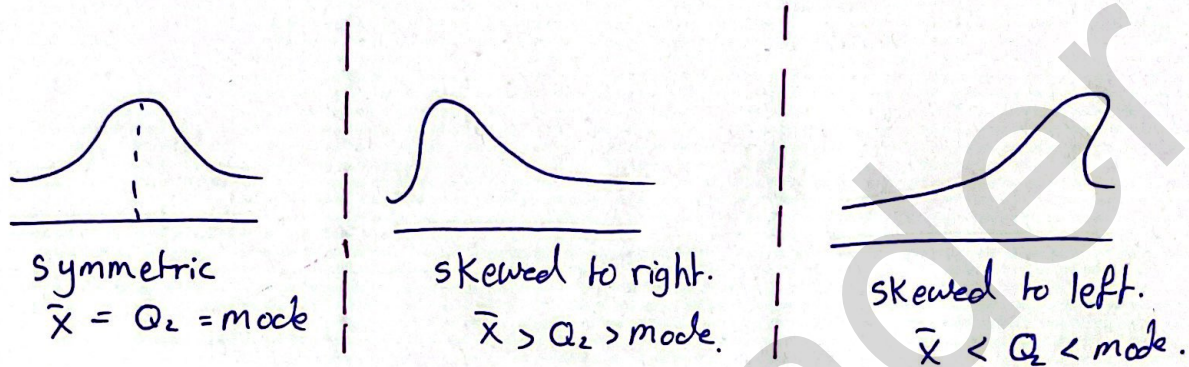
2] coefficient of variation :

$C.V = \frac{S}{\bar{X}} * 100\%$  → كل ما زاد بزيء النسبة .

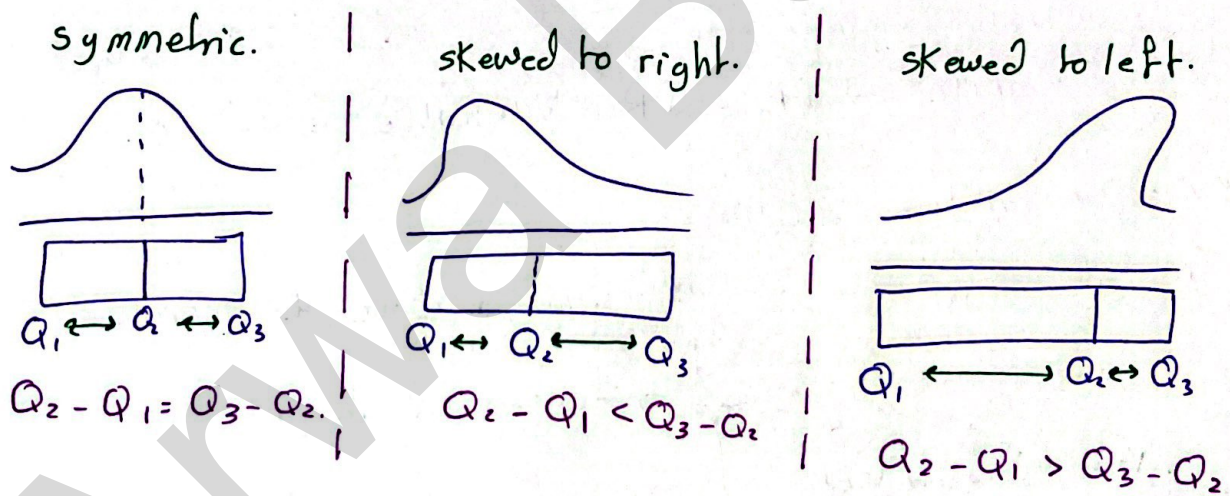
\* Skewness :

we have 3 Methods :-

1] By Measures of central tendency :-



2] By Quarhiles (Box-plot) :-

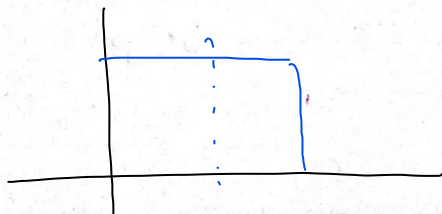


3] By Pearson's Index :-

→ compute  $P = \frac{3(\bar{X} - Q_2)}{S}$

$P > 0 \rightarrow$  skewed to right.  
 $P < 0 \rightarrow$  skewed to left  
 $P = 0 \rightarrow$  symmetric.

\* Note :



uniform  
= symmetric

## \* Linear Transform (coding) :

الموضوع المطلوب والله

$$\underbrace{y}_{\text{new measure}} = a \cdot \underbrace{x}_{\text{old measure}} + b$$

, a, b : any numbers.

1] For Measures of central tendency :

\* يتأثر بالهزب والجمع

$$1) \bar{y} = a \cdot \bar{x} + b.$$

$$2) Q_2(y) = a \cdot Q_2(x) + b$$

$$3) \text{mode}(y) = a \cdot \text{mode}(x) + b$$

2] For Measures of variation :

\* يتأثر بالهزب فقط وبعده موجب

$$1) \text{Range}(y) = |a| \cdot \text{Range}(x)$$

$$2) \text{IQR}(y) = |a| \cdot \text{IQR}(x)$$

$$3) \text{IPR}(y) = |a| \cdot \text{IPR}(x)$$

$$4) S_y = |a| \cdot S_x$$

$$5) S_y^2 = a^2 \cdot S_x^2$$

3] For other Measures :

$$1) P_k(y) = a \cdot P_k(x) + b, \quad a > 0.$$

$$P_k(y) = a \cdot P_{(100-k)}(x) + b, \quad a < 0.$$

\* إذا  $a$  موجبة يأخذ نفس النسبة أما إذا سالبة يأخذ مقابلة النسبة

$$2) Q_1(y) = a \cdot Q_1(x) + b, \quad a > 0.$$

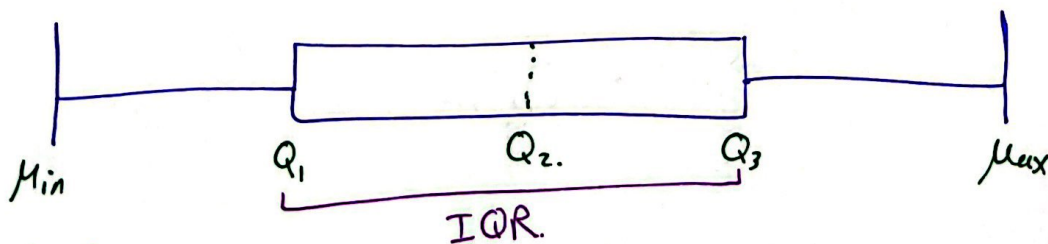
$$Q_1(y) = a \cdot Q_3(x) + b, \quad a < 0.$$

$$3) Q_3(y) = a \cdot Q_3(x) + b, \quad a > 0.$$

$$Q_3(y) = a \cdot Q_1(x) + b, \quad a < 0.$$

## \* Data representation :

1] Box & whiskers plot :



↳ five-number-summary : Min, Q<sub>1</sub>, Q<sub>2</sub>, Q<sub>3</sub>, Max.

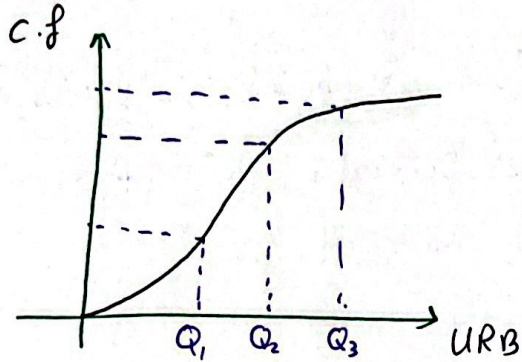
2] Pie-chart :- represents x & f.

find the angles :-

$$\theta = \frac{f}{\sum f} * 360^\circ.$$

3] C.f curve (O-give) :-  
represent c.f & URB.

50



۴۰  
کثیر نسبتہ کیف  
ترجع الرحمة لجدول.

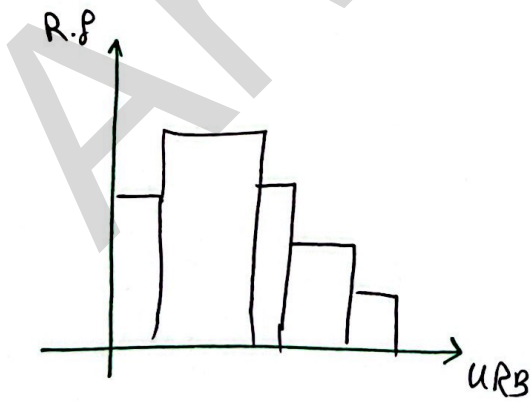
4] Histogram :-  
represents URB & frequency.

50



۴۰  
نفر ف کیف  
ترجع الرحمة إلى  
جدول.

Sometimes we represent. URB & relative frequency.



بعض الاحیان يمثل ال U.R.B.  
مع التكرار النسبي.

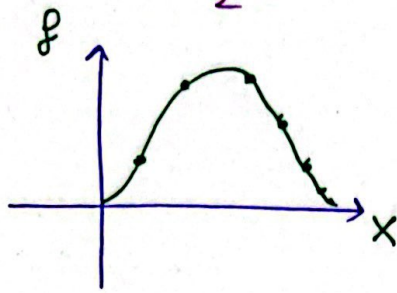
انتبه على axis -y هو يمثل.

11

5 Polygon :-

represents X & frequency, X is the midpoint.

$$X = \frac{\text{lower} + \text{upper}}{2}$$



6 Dot-plot :-

represents X & frequency.



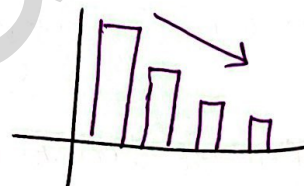
7 Bar-graph & Pareto chart :-

→ represents X & frequency.

→ In Pareto-chart, we put frequency in ascending order.  
لم يرتب القيم تناهدي وبعدها بتل.



Bar-graph



Pareto-chart.

8 Time-series-chart :-

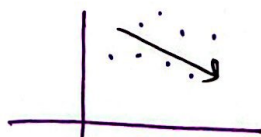
من اسمه يعني بتراقب زيادة أو نقصان خلال مدة زمنية.

9 Scatter-diagram :-

represent relationship between X & y.



Positive correlation



negative correlation.

\* Notes :-

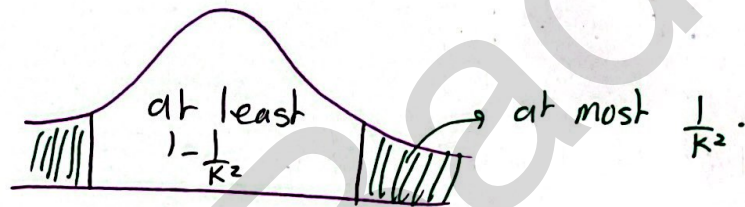
→ For qualitative data (نوعية), we can use :-

Pie chart, Bar graph & Pareto chart only.

\* بالامتحان مارج ترسم فقط حيكونا مطلوب توجب شي معين  
من رسمه لهيك لازم تعرف كيف ترجع الرسمه لجدول.  
[شيك اسئلة التيت بانك وال sheets.]

\* Cheby shev's theorem :-

The proportion of observations within  $K$  standard deviation from the mean :-



For any set of data:

At least  $1 - \frac{1}{K^2}$  within  $(\bar{x} - K \cdot s, \bar{x} + K \cdot s)$

At most  $\frac{1}{K^2}$  outside  $(\bar{x} - K \cdot s, \bar{x} + K \cdot s)$

no. of obs.  $\Leftrightarrow$  Percentage  $\Leftrightarrow K \Leftrightarrow$  Interval  
عدد مشاهدات  $\Leftrightarrow$  نسبة  $\Leftrightarrow$  فترة

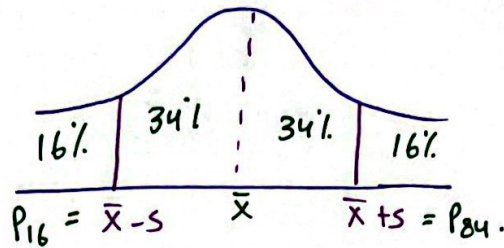
\* number of obs = percentage \* n.

→ whole no.  $\rightarrow$  1 ترقي  
→ fraction  $\rightarrow$  at least round up.  
→ at most round down.

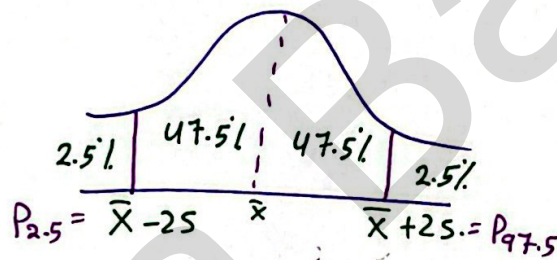
\* Empirical Rule:

For Bell-shaped data only.

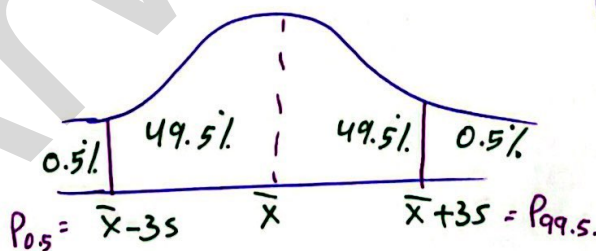
1 For  $K=1 \rightarrow (\bar{x}-s, \bar{x}+s)$  contains at least 68%



2 For  $K=2 \rightarrow (\bar{x}-2s, \bar{x}+2s)$  contains at least 95%



3 For  $K=3 \rightarrow (\bar{x}-3s, \bar{x}+3s)$  contains at least 99%



رجعنا اللتب بتعلي  
99.7% بس مش  
مات

عدد الملاحظات  $\leftrightarrow$  نسبة  $\leftrightarrow$  قيم  $\leftrightarrow$  Interval  
no. of obs  $\leftrightarrow$  Percentage  $\leftrightarrow$  K  $\leftrightarrow$  فترة

\* Number of observations = Percentage \* n.

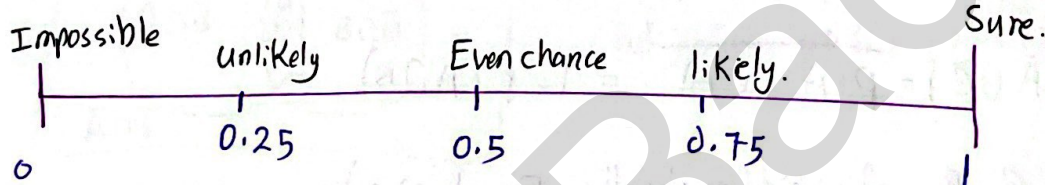


## \* Chapter (3) :- Elements of probability

→ Event :- Any subset of the sample space, denoted by A, B, C, ...

- ① Simple. → one element only.
- ② Combined → two or more.
- ③ Sure → All the sample space.
- ④ Impossible. → No elements of S.

$$P(A) = \frac{N(A)}{N(S)}$$



\* Note :- Any has prob less than 0.05 called unusual.

→ Facts :-

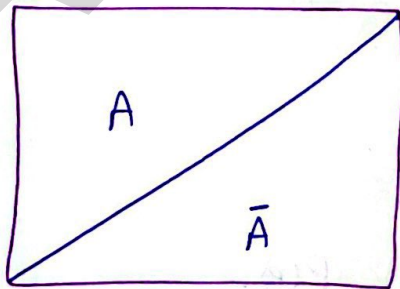
①  $P(S) = 1$

②  $P(\phi) = 0$

③  $0 \leq P(A) \leq 1$

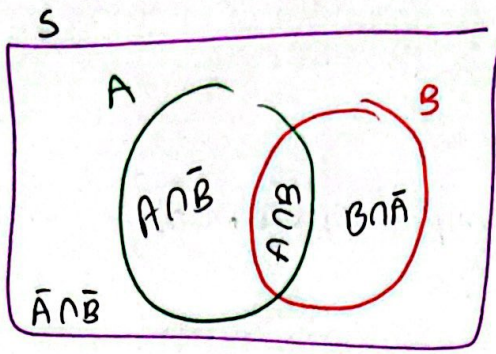
\* Rules of probability :-

1)



□  $P(A) = 1 - P(\bar{A})$  OR  $P(\bar{A}) = 1 - P(A)$ .

2)



تبدیلیت

$$A \cap B = B \cap A$$

$$A \cup B = B \cup A$$

$$2) P(A \cap \bar{B}) = P(A) - P(A \cap B)$$

$$3) P(B \cap \bar{A}) = P(B) - P(A \cap B)$$

$$4) P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

5) Demorgan Law's :-

$$1. P(\bar{A} \cap \bar{B}) = \overline{P(A \cup B)} = 1 - P(A \cup B)$$

$$2. P(\bar{A} \cup \bar{B}) = \overline{P(A \cap B)} = 1 - P(A \cap B)$$

6) A & B disjoint (mutually Exclusive) :-

$$P(A \cap B) = 0$$

التقاطع صفر



7) A & B Independent :-

$$P(A \cap B) = P(A) \cdot P(B)$$

التقاطع حاصل ضرب

8) Conditional probability :-

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

given  
if

\* If they're independent :-

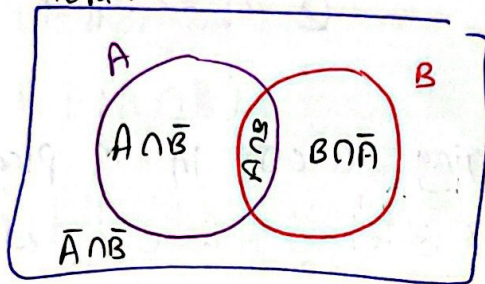
$$P(A|B) = P(A) \quad \& \quad P(B|A) = P(B)$$

\* Prob. table \*

	A	$\bar{A}$	total
B	$P(A \cap B)$	$P(B \cap \bar{A})$	$P(B)$
$\bar{B}$	$P(A \cap \bar{B})$	$P(\bar{A} \cap \bar{B})$	$P(\bar{B})$
tot	$P(A)$	$P(\bar{A})$	1

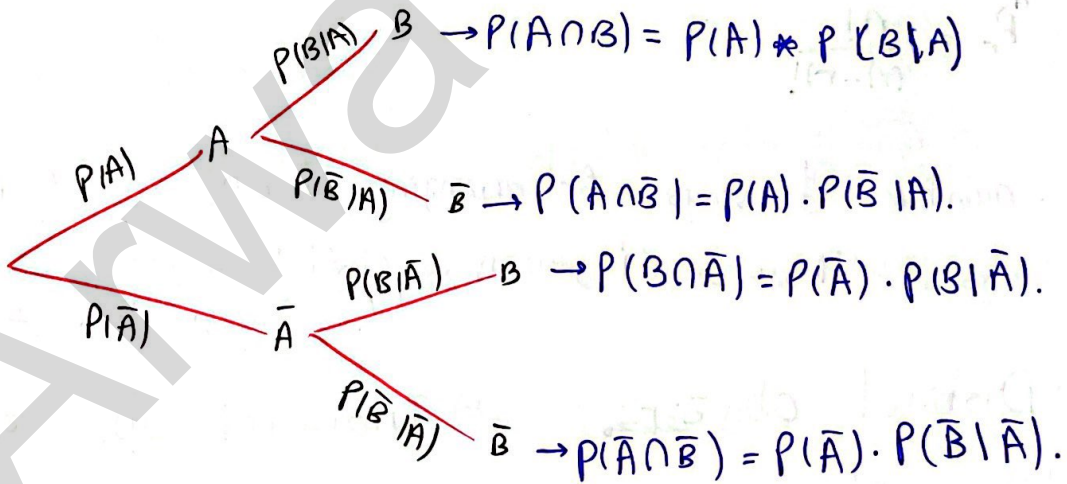
يمكن الجدول يكون  
على أرقام قطع.

\* Venn-Diagram:-  
total.



لما ينقسم المجموعة إلى  
جزئنا، بينهم عناصر مشتركة.

\* Tree diagram \*



$\leftarrow$  لما ينقسم الفضاء العيني مرتين  
 $\leftarrow$  لما اختار عنصرين  
 $\leftarrow$  لما اتفقت تجربة على مرحلتين

## \* Counting Rules:

## یا ستر ارب

### 1] Multiplication principle:

$$\boxed{n_1} \quad \boxed{n_2}$$

$$\text{total } n = n_1 * n_2.$$

### 2] Factorial:

$$n! = n(n-1)(n-2) \dots (2)(1).$$

### \* Note s

$$\text{① } 0! = 1$$

$$\text{② } 1! = 1$$

$$\text{③ } 2! = 2.$$

$n!$ : number of ways for arranging  $n$  obj in  $R$  places.

له ترتيب عناصر في أماكن، عدد العناصر مساوي لعدد الأماكن  
وما عندي شروط على الخانات.

### 3] Permutation :-

$${}^n P_r = \frac{n!}{(n-r)!}$$

${}^n P_r$ : number of ways for arranging  $n$  obj in  $r$  places.

له ترتيب عناصر في أماكن، عدد العناصر أكبر من عدد الأماكن وما عندي  
شروط على الخانات.

A) Distinct obj مختلفة

$${}^n P_r = \frac{n!}{(n-r)!}$$

B) Indistinct obj متكررة

$$P = \frac{n!}{n_1! n_2! \dots n_r!}$$

4] combination :-

$${}^n C_r = \binom{n}{r} = \frac{n!}{(n-r)! \cdot r!} = \frac{{}^n P_r}{r!}$$

${}^n C_r$ : number of ways for selecting r obj from n obj  
لـ اختيار عناصر بدون ترتيب وبدون ارجاع

- \* انتبه لنوع السؤال اذا بطلب احتمالية أو عدد الحركات .
- \* اذا في شروط على الخانات بطلع الناتج ارقام مصنوعة ببعض

\* Note:  $\binom{n}{r} = \binom{n}{n-r}$

GOOD LUCK!

T. Arwa M. Bader