

The University of Jordan / Physics Department

Grancoli, 7<sup>th</sup> edition / Solutions to  
Extra Problems

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6] AF : antifreeze  
mix : mixture.

$$\rho_{\text{mix}} = \frac{\rho_{\text{AF}} V_{\text{AF}} + \rho_w V_w}{V_{\text{mix}}} \quad m_{\text{mix}}$$

$$\begin{cases} V_{\text{AF}} = 4 \text{ L} \\ V_w = 5 \text{ L} \end{cases}$$

$$= \frac{\rho_{\text{AF}} V_{\text{AF}} + \rho_w V_w}{V_{\text{mix}}}$$

$$SG_{\text{mix}} = \frac{\rho_{\text{mix}}}{\rho_w} = \frac{SG_{\text{AF}} V_{\text{AF}} + V_w}{V_{\text{mix}}} = \frac{(0.8)(4 \text{ L}) + 5 \text{ L}}{9 \text{ L}}$$

$$\therefore SG_{\text{mix}} = \frac{8.2 \text{ L}}{9 \text{ L}} = 0.91$$

(3)

Pressure inside lungs =  $P_{in} = P_{atm}$

Pressure outside lungs =  $P_{out}$

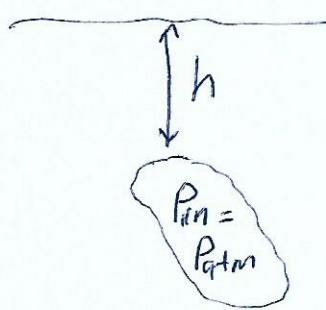
$$P_{out} = P_{atm} + \rho_w g h$$

$$\Delta P = P_{out} - P_{in} = P_{atm} + \rho_w g h - P_{atm}$$

$$\Delta P = \rho_w g h$$

$$\therefore h = \frac{\Delta P}{\rho_w g} = \frac{85 \text{ mm Hg} \times \frac{1.013 \times 10^5}{760 \text{ mm Hg}}}{1000 \times 9.8}$$

$$h = 1.156 \text{ m} \approx 1.16 \text{ m}$$



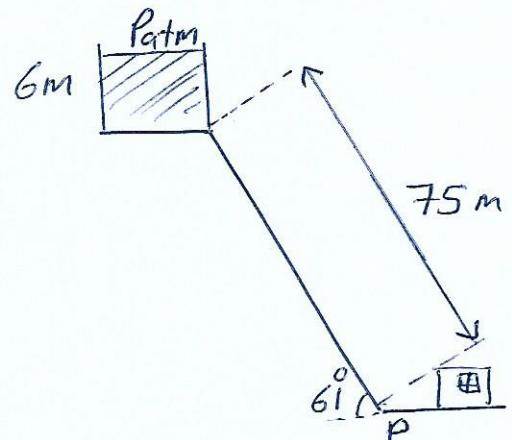
(7)

$$\textcircled{a}) P = P_{atm} + \rho g (6) + \rho g (75 \sin 61^\circ)$$

$$P_{gauge} = P - P_{atm} = \rho g [6 + 75 \sin 61^\circ]$$

$$P_{gauge} = (1000)(9.8)[6 + 75 \sin 61^\circ]$$

$$P_{gauge} = 701645 \text{ Pa}$$



- \textcircled{b}) Ignoring friction forces the water cannot exceed the top of the tank by conservation of mechanical energy.

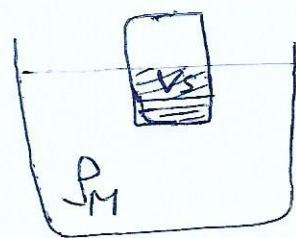
$$\therefore h_{max} = 75 \sin 61^\circ + 6 \approx 71.6 \text{ m.}$$

$$23] \frac{P_o}{P_F} = \frac{V_s}{V}$$

$$\frac{V_s}{V} = \frac{7.8 \times 10^3}{13.6 \times 10^3} \approx 0.57$$

$$\Rightarrow \text{required fraction } \frac{V_s}{V} = 0.57$$

i.e 57% of the volume will be below the surface of the mercury.

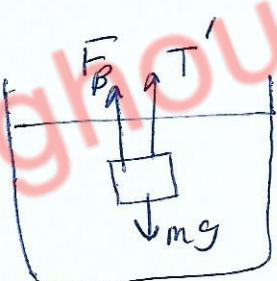


O: object (iron)  
F: Fluid (Mercury)

$$24] F_B + T' = mg$$

$$F_B = mg - T' = P_w V g$$

$$\therefore V = \frac{mg - T'}{P_w g} = \frac{9.28 g - 6.18 g}{1000 g}$$



Note:  $T'$  is the apparent weight in water = 6.18 g  
 $V$  is the volume of the displaced fluid = volume of the mass as it is fully under water.

$$V = 0.0031 \text{ m}^3$$

$$P_{\text{mass}} = \frac{9.28 \text{ kg}}{0.0031 \text{ m}^3} = 2993.5 \text{ kg/m}^3$$

30] displaced volume =  $69.6 \text{ L} = 69.6 \times 10^{-3} \text{ m}^3$  [4]

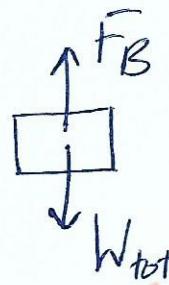
$F_b$  = weight of displaced fluid

$$F_b = \rho_w (69.6 \times 10^{-3}) g \approx 682 \text{ N}$$

$$W_{\text{total}} = M_{\text{total}} g = 72.8 g \approx 713 \text{ N}$$

Since  $W_{\text{total}} > F_b \Rightarrow$

diver will sink.



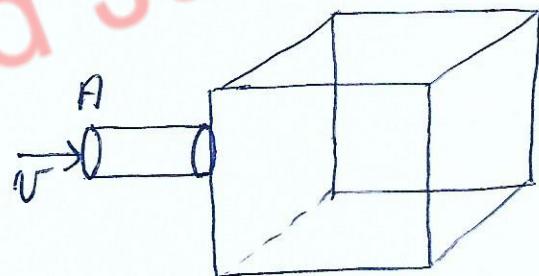
37] every 12 min a volume of air = 143.5 enters the room through the duct.

Volume flow rate =  $\frac{\Delta V}{\Delta t}$

$$\frac{\Delta V}{\Delta t} = A U$$

$$\frac{143.5 \text{ m}^3}{12 \times 60 \text{ s}} = 0.1993 \frac{\text{m}^3}{\text{s}} = A U$$

$$\therefore U = \frac{0.1993 \text{ m}^3/\text{s}}{\pi (0.12)^2 \text{ m}^2} \approx 4.4 \text{ m/s}$$



$$\begin{aligned} \text{Volume of room} \\ = 8 \cdot 2 \times 5 \times 3.5 \text{ m}^3 \\ = 143.5 \text{ m}^3 \end{aligned}$$

43] At points 1 and 2

the velocities  $v_1$  and  $v_2$   
are zero. Pressure is

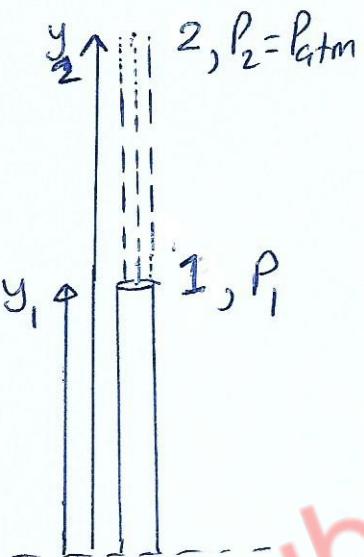
needed for water to acquire  
velocity at point 1.

$$P_1 + \rho gy_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho gy_2 + \frac{1}{2} \rho v_2^2$$

$$P_1 + \rho gy_1 + 0 = P_{atm} + \rho gy_2 + 0$$

$$P_1 - P_{atm} = \rho g (y_2 - y_1)$$

$$= (1000)(9.8)(16) = 1.56 \times 10^5 \text{ Pa}$$



44] Since  $y_u \approx y_d \Rightarrow \rho gy_u = \rho gy_d$

Apply Bernoulli's eqn to upper  
and lower regions as shown:

$$P_u + \frac{1}{2} \rho v_u^2 + \rho gy_u = P_d + \frac{1}{2} \rho v_d^2 + \rho gy_d$$

Assume air inside house to have zero speed  $\Rightarrow v_d = 0$ .

while  $v_u = 180 \times \frac{1000}{3600} = 50 \text{ m/s} \Rightarrow P_u < P_d$  and

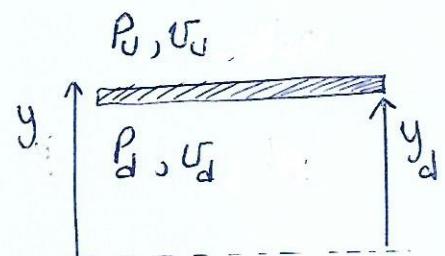
so a net lifting force is  $(P_d - P_u) A$

Need to find  $P_d - P_u$ .

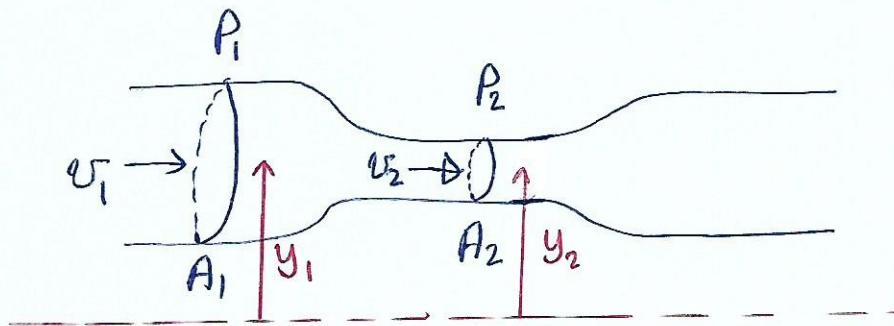
$$\frac{1}{2} \rho (v_u^2 - v_d^2) = P_d - P_u \Rightarrow P_d - P_u = \frac{1}{2} (1.29) (50^2 - 0) = 1612.5 \text{ Pa}$$

just to lift the roof  $Mg = (P_d - P_u) A = 1612.5 \times 6.2 \times 12.4 = 123969 \text{ Newton.}$

$\Rightarrow$  weight of roof  $Mg \approx 1.24 \times 10^5 \text{ N.}$



50] Venturi tube is used to measure the flow speed of liquids and gases. L6



$$\text{continuity equation} \Rightarrow A_1 v_1 = A_2 v_2 - \textcircled{1}$$

Bernoulli's equation:

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2 - \textcircled{2}$$

$$y_1 = y_2 \Rightarrow \rho g y_1 = \rho g y_2$$

$$\therefore P_1 - P_2 = \frac{1}{2} \rho (v_2^2 - v_1^2) \quad \left[ \begin{array}{l} \text{NOTE: } P_1 > P_2 \\ \text{as } v_1 < v_2 \end{array} \right]$$

$$\text{from } \textcircled{1} \quad v_2 = \frac{A_1}{A_2} v_1$$

Substitute for  $v_2$  in eq. \textcircled{2} we get

$$P_1 - P_2 = \frac{1}{2} \rho \left( \frac{A_1^2}{A_2^2} - 1 \right) v_1^2 = \frac{1}{2} \rho \times \frac{1}{A_2^2} (A_1^2 - A_2^2) v_1^2$$

$$\therefore 2A_2^2 (P_1 - P_2) = \rho (A_1^2 - A_2^2) v_1^2$$

$$\Rightarrow v_1 = A_2 \sqrt{\frac{2(P_1 - P_2)}{\rho(A_1^2 - A_2^2)}}$$

so, if we know  $A_1, A_2, P_1$  and  $P_2$  we can determine the flow speed  $v_1$ .

47] assume the heights of bottom and top surfaces of the wing to be the same.

$$\Rightarrow \rho g y_1 = \rho g y_2$$

$$\frac{\textcircled{2} P_2, v_2}{\textcircled{1} P_1, v_1} \text{ wing}$$

----- ground

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

$$v_2 = 280 \text{ m/s} > v_1 = 150 \text{ m/s}$$

$$\Rightarrow P_2 < P_1$$

$$\begin{aligned} P_1 - P_2 &= \frac{1}{2} \rho (v_2^2 - v_1^2) \\ &= \frac{1}{2} (1.29) ((280)^2 - (150)^2) = 36055.5 \text{ Pa} \end{aligned}$$

$$\text{lifiting force} = (P_1 - P_2) A \stackrel{\text{wing's area}}{\uparrow} = (P_1 - P_2)(88)$$

$$\therefore \text{lifiting force } F_L = (36055.5)(88) \approx 3.173 \times 10^6 \text{ N.}$$

## Additional Problem

A collapsible plastic bag contains glucose solution. If the average gauge pressure in the vein is  $1.33 \text{ kPa}$ , what must be the minimum height  $h$  of the bag in order to infuse glucose into the vein?

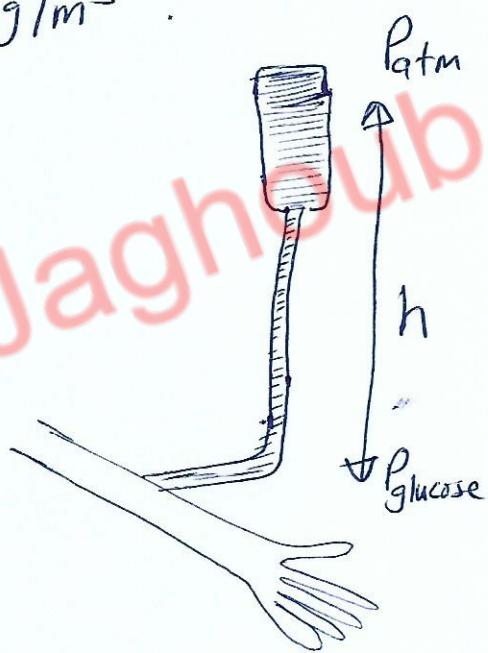
$$\text{Assume } SG_{\text{glucose}} = 1.02$$

$$\Rightarrow \rho_{\text{glucose}} = 1.02 \times \rho_w = 1020 \text{ kg/m}^3.$$

$$P_{\text{glucose}} = P_{\text{atm}} + \rho_{\text{glucose}} g h$$

$$P_{\text{glucose}} - P_{\text{atm}} = \rho_{\text{glucose}} g h$$

$$\underbrace{\rho_{\text{glucose}}}_{\text{gauge}} = \rho_{\text{glucose}} g h$$



for glucose to be infused into the vein  $\Rightarrow$

$$\rho_{\text{glucose}} \geq \rho_{\text{blood}}$$

$$\rho_{\text{glucose}} g h \geq 1.33 \times 10^3$$

$$\therefore h = \frac{1.33 \times 10^3}{1020 \times 9.8} \sim 0.133 \text{ m.}$$